## Write your name here



## Mathematics

Paper 2 (Calculator)
Aiming for 7
Higher Tier

## Spring 2023 Practice Paper Time: 1 hour 30 minutes

You must have: Ruler graduated in centimetres and millimetres,
Total Marks protractor, pair of compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.

Instructions

- Use black ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Answer the questions in the spaces provided
- there may be more space than you need.
- You must show all your working.
- Diagrams are NOT accurately drawn, unless otherwise indicated.
- Calculators may be used.
- If your calculator does not have a $\pi$ button, take the value of $\pi$ to be 3.142
unless the question instructs otherwise.


## Information

- The total mark for this paper is 80 . There are 22 questions.
- Questions have been arranged in an ascending order of mean difficulty, as found by students achieving Grade 7 in the Summer and November 2022 examinations.
- The marks for each question are shown in brackets - use this as a guide as to how much time to spend on each question.


## Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.


## Answer ALL TWENTY FOUR questions. <br> Write your answers in the spaces provided. <br> You must write down all the stages in your working.

1 Ella invests $£ 7000$ for 2 years in an account paying compound interest.
In the first year, the rate of interest is $3 \%$
In the second year, the rate of interest is $1.5 \%$
Work out the value of Ella's investment at the end of 2 years.

2 A box in the shape of a cuboid is placed on a horizontal floor. The box exerts a force of 180 newtons on the floor. The box exerts a pressure of 187.5 newtons $/ \mathrm{m}^{2}$ on the floor.

$$
\text { pressure }=\frac{\text { force }}{\text { area }}
$$

The face in contact with the floor is a rectangle of length 1.2 metres and width $x$ metres.
Work out the value of $x$.

$$
x=
$$

$\qquad$

3 A new phone cost $£ 679$
The value of the phone decreases at a rate of $4 \%$ per year.
Work out the value of the phone at the end of 3 years.

4 Chanda buys a necklace for $£ 120$
She sells the necklace for $£ 135$
Work out her percentage profit.

5


Work out the value of $x$.
Give your answer correct to 3 significant figures.

$$
x=.
$$

$\qquad$

6 In Spain, Sam pays 27 euros for 18 litres of petrol.
In Wales, Leo pays $£ 40.80$ for 8 gallons of the same type of petrol.
1 euro $=£ 0.85$
4.5 litres $=1$ gallon

Sam thinks that petrol is cheaper in Spain than in Wales.
Is Sam correct?
You must show how you get your answer.

7 Saffron wants to work out an estimate for the total number of fish in a lake.
On Friday, Saffron catches 180 fish from the lake.
She puts a tag on each of these fish and puts them back into the lake.
On Saturday, Saffron catches 305 fish from the same lake.
She finds that 45 of the 305 fish are tagged.
Work out an estimate for the total number of fish in the lake.

8 The equation of the line $\mathbf{L}_{\mathbf{1}}$ is $y=2 x+3$
The equation of the line $\mathbf{L}_{2}$ is $5 y-10 x+4=0$
Show that these two lines are parallel.

9 Festival A will be in a rectangular field with an area of $80000 \mathrm{~m}^{2}$
The greatest number of people allowed to attend Festival A is 425
Festival B will be in a rectangular field 700 m by 2000 m .
The greatest number of people allowed to attend Festival B is 6750
The area per person allowed for Festival B is greater than the area per person allowed for Festival A.
(a) How much greater?

Give your answer correct to the nearest whole number.

Callum says,
" $300 \mathrm{~cm}^{2}$ is the same as $3 \mathrm{~m}^{2}$ because there are 100 cm in 1 m so you divide by 100 "
Callum's method is wrong.
(b) Explain why.
$\qquad$
$\qquad$
$\qquad$
(a) Simplify $\left(x^{3}\right)^{5}$
(b) Expand and simplify $4(x+3)+7(4-2 x)$
(c) Factorise fully $15 x^{3}+3 x^{2} y$

11 The scatter graph shows information about the amount of rainfall, in mm, and the number of hours of sunshine for each of ten English towns on the same day.


One of the points is an outlier.
(a) Write down the coordinates of this point.
$\qquad$
(b) Ignoring the outlier, describe the relationship between the amount of rainfall and the number of hours of sunshine.
$\qquad$
$\qquad$
$\qquad$

On the same day in another English town there were 7 hours of sunshine.
(c) Using the scatter graph, estimate the amount of rainfall in this town on this day.

12 The length of a football pitch is 90 metres, correct to the nearest metre.
Complete the error interval for the length of the football pitch.

13 Here is the graph of $y=x^{2}-6 x+4$

(a) Write down the $y$ intercept of the graph of $y=x^{2}-6 x+4$
$\qquad$
(b) Write down the coordinates of the turning point of the graph of $y=x^{2}-6 x+4$
$\qquad$
(c) Use the graph to find estimates for the roots of $x^{2}-6 x+4=0$

14 Kieron has 13 workers he can use for a job.
He knows that 6 workers would take $14 \frac{1}{2}$ days to complete this job.
Show that Kieron has enough workers to finish this job in less than 7 days.

15 Using algebra, prove that $1.06 \dot{2}$ can be written as $1 \frac{14}{225}$

16 Use your calculator to work out

$$
\frac{\sqrt[3]{1.57^{4}+\tan 60^{\circ}}}{7.2^{\frac{1}{2}}}
$$

Give your answer correct to 3 significant figures.

17 Here are the equations of two straight lines.

$$
y=\frac{1}{2} x-6 \quad 6 y=3 x+7
$$

Oscar says that these lines are parallel.
Is Oscar correct?
You must give a reason for your answer.
$\qquad$
$\qquad$
$\qquad$

18 Here are the first five terms of an arithmetic sequence.
713
19
25
31
(a) Find an expression, in terms of $n$, for the $n$th term of this sequence.
$\qquad$

The $n$th term of a different sequence is $8-6 n$
(b) Is -58 a term of this sequence?

You must show how you get your answer.

19 The diagram shows a plan of Jason's garden.
$A B C O$ and $D E F O$ are rectangles.
$C D O$ is a right-angled triangle.
$A F O$ is a sector of a circle with centre $O$ and angle $A O F=90^{\circ}$


Jason is going to cover his garden with grass seed.
Each bag of grass seed covers $14 \mathrm{~m}^{2}$ of garden.
Each bag of grass seed costs $£ 10.95$
Work out how much it will cost Jason to buy all the bags of grass seed he needs.

20 Faiza is studying the population of rabbits in a park.
She wants to estimate the number of rabbits in the park.
On Monday she catches a random sample of 20 rabbits in the park, marks each rabbit with a tag and releases them back into the park.

On Tuesday she catches a random sample of 42 rabbits in the park.
12 of the rabbits are marked with a tag.
(a) Find an estimate for the number of rabbits in the park.

Albie is studying the population of rabbits in a wood.
One day, he catches 55 rabbits and finds that 40 of these rabbits are marked with a tag. Albie estimates there are 50 rabbits in the wood.
(b) Explain why Albie's estimate cannot be correct.
$\qquad$
$\qquad$
$\qquad$

21 In an experiment, 60 students each completed a puzzle.
The cumulative frequency graph shows information about the times taken for the 60 students to complete the puzzle.


For these 60 students,
the least time taken was 24 seconds
the greatest time taken was 96 seconds.
On the grid below, draw a box plot for the distribution of the times taken by the students.

(Total for Question 21 is $\mathbf{3}$ marks)

22 Here is a triangle.


Work out the area of the triangle.
Give your answer correct to 3 significant figures.
$\mathrm{cm}^{2}$
$23 P Q R$ and $Q R S$ are triangles.


Calculate the length of $Q S$.
Give your answer correct to 3 significant figures.
You must show all your working.
cm

24 The box plot shows information about the sales, in thousands of pounds (£000s), of an online store each month.


Andrew says,
"Three quarters of the given data lies between 160000 and 350000 because these are the values of the lower quartile and the upper quartile."

Andrew is wrong.
(a) Explain why.
$\qquad$
$\qquad$
$\qquad$

The table shows information about the sales, in $£ 000$ s, in a shop each month.

|  | Sales (£000s) |
| :--- | :---: |
| least value | 30 |
| lower quartile | 80 |
| median | 170 |
| upper quartile | 260 |
| greatest value | 350 |

(b) On the grid below, draw a box plot for this information.

(c) Compare the distribution of the sales of the online store with the distribution of the sales in the shop.

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